

1
2 **TIME TRENDS IN THE EUROPEAN AVERAGE TEMPERATURE**
3 **ANOMALIES FOR THE PERIOD 1655-2017**

4 **Luis A. Gil-Alana, University of Navarra, Pamplona, Spain**

5 **and**

6 **Carmen Lafuente, University Francisco de Vitoria, Madrid, Spain**

7
8
9 **ABSTRACT**

10 This paper deals with the analysis of the time trends for the European average
11 temperature anomalies for the period from 1655 to 2017 using a dataset that is based on
12 the Central England Temperatures (CET) and other meteorological stations. The results
13 indicate that the series display long memory behavior and based on this and using
14 recursive methods, we find that the time trend becomes statistically significant when
15 incorporating the data from 2010 onwards suggesting the importance of the last few
16 years in the claim for warming.

17 **Keywords:** European temperature anomalies; time trends; persistence; long memory

18
19
20
21 **Corresponding author:** Professor Luis A. Gil-Alana
22 University of Navarra
23 Faculty of Economics and NCID
24 31080 Pamplona
25 SPAIN

26
27
28 Email: alana@unav.es

29
30
31
32 Luis A. Gil-Alana gratefully acknowledges financial support from the Ministerio de Economía y
33 Competitividad (ECO2017-85503-R). Comments from the Editor are gratefully acknowledged.

35 **1. Introduction**

36 This paper deals with the analysis of the temperatures in Europe. More in particular, we
37 focus on the analysis of the time trends to check if there has been an increase in the
38 values across time. For the estimation of the time trends a usual requirement is that the
39 errors in the regression model must be well behaved and it is here where we make our
40 initial contribution by allowing the errors to be fractionally integrated, a feature that has
41 been observed in many climatological data.

42 Some authors have analyzed the time trends in climatological data by classifying
43 the global land into various climatic regions based on the climatological annual
44 precipitation (Zhou et al. 2009). These authors analyze the spatial dependence of annual
45 diurnal temperature range (DTR) trends from 1950–2004 on the annual climatology of
46 three variables: precipitation, cloud cover, and leaf area index (LAI). It is found that the
47 regional average trends for annual minimum temperature (T_{\min}) and DTR exhibit
48 significant spatial correlations with the climatological values of these three variables,
49 while such correlation for annual maximum temperature (T_{\max}) is very weak.

50 Focussing on Europe, there are other studies on time trends of climatological
51 data. Klein & Können (2003), for example, studied the trends of extreme temperature
52 indices on the basis of daily series of temperature and precipitation from more than 100
53 meteorological stations in Europe. The selected indices of daily temperature and
54 precipitation extremes showed pronounced trends within the 1946–99 period. Europe-
55 average trends in mean temperature are accompanied by “asymmetric” rather than
56 “symmetric” changes in temperature extremes for two consecutive periods: 1946–75
57 and 1976–99. Luterbacher et al. (2004) argued that for the 21st-century European
58 climate is very likely warmer than that of any other time during the past 500 years.
59 Moberg & Jones (2005) analyzed 20th century trends in six indices for precipitation and

60 four indices for temperature extremes, calculated from daily observational data for 80
61 European stations situated across central and western Europe. The selected indices
62 reflected rather moderate extremes.

63 According to Mariani & Zavatti (2017) Europe is the world region with the
64 longest time series of instrumental data due to the fact that the first meteorological
65 instruments (thermometer, pluviometer, evaporimeter and barometer) were invented by
66 some scientists of the Galilean school (Accademia del Cimento). In this paper we use
67 the dataset gathered by these authors with the aim of organizing an easily updatable
68 dataset which allows us to present an overview of the trend of European climate over
69 the long time periods covered by instrumental data. The dataset includes information
70 from 29 stations and starts in 1655 which is just the beginning of the Florentine Galileo
71 series data (Camuffo & Bertolin 2012). The Central England Time Series, CET
72 (MetOffice_Hadley Centre, 2016) was added from year 1659 and gradually other
73 stations joined (MeteoFrance, ECA&D, MeteoSwiss), at first coming from historical
74 observatories (Camuffo & Jones 2002) and then from current operational networks. The
75 most recent data were obtained from either the website Rimfrost (2016) and from the
76 above mentioned stations (Mariani & Zsavatti 2017). (See the Appendix for a
77 description of the stations used).

78 Global air temperature has become the primary metric for judging global
79 climate change. There are many studies on the temperature trend over time. Many of
80 these studies explain the causes of global warming. Andronova & Schlesinger (2000)
81 analyze two types of factors: "external" factors of human (anthropogenic) activity,
82 volcanoes and putative variations in the irradiance of the sun, and the "internal" factor
83 of natural variability. They show that temperature changes for different state-of-the-art
84 radiative forcing models, "the anthropogenic effect has steadily increased in size during

85 the entire 20th century such that it presently is the dominant external forcing of the
86 climate system, there is a residual factor at work within the climate system, whether a
87 natural oscillation or something else as yet unknown”.

88 Kaufmann et al (2011) indicate that observed temperature after 1998 is
89 consistent with the current understanding of the relationship among global surface
90 temperature, internal variability, and radiative forcing, which includes anthropogenic
91 factors but too must be considered and the changes in natural variables. Some studies on
92 temperature in Europe show that “Europe's temperature rise of about 1°C since the
93 1980s is considerably larger than expected from anthropogenic greenhouse warming”
94 (Philipona et al. 2009).

95 More in line with our work, Lovsletten and Rypdal (2016) use a model
96 containing a linear deterministic trend along with a long memory process that is
97 specified using various alternatives, including a Gaussian noise model. Their results
98 indicate evidence of linear time trend and long memory in the majority of the regional
99 temperature series examined.¹

100 External and internal factors influence changes in temperature but although
101 external factors are controlled, there are other factors that influence climate change. Our
102 research focuses on studying whether temperature, with data coming back to 1655, have
103 really increased without considering its causes.

104 We use the abovementioned dataset to examine two important features observed
105 in the temperatures, such as the degree of persistence, measured in terms of the
106 fractional differencing parameter, and the potential warming, measured by means of a
107 (linear) time trend coefficient. We show in the following section that both issues are
108 very much related since the estimation of the time trend coefficient clearly depends on

¹ A Bayesian approach of long memory (fractional Gaussian noise) with a linear trend can be found in Myrvoll-Nielsen et al. (2017).

109 the correct specification of the error term, which is allowed to be fractionally integrated
110 to permit some degree of persistence. It might be argued that a linear trend may be
111 unrealistic with a time horizon of about 400 years; nevertheless, it appears as a natural
112 statistical instrument to measure warming. Our results can be summarized as follows:
113 evidence of long memory behavior (with an order of integration in the stationary range
114 $(0, 0.5)$) is observed in the European average temperature anomalies, and based on this
115 pattern, a positive time trend is found to be statistically significant. This time trend
116 coefficient is slightly higher than the one obtained under $I(0)$ (or short memory)
117 behavior. Testing if these two features, persistence and time trend, have changed across
118 time, our results indicate that the degree of persistence has increased across time,
119 especially after 1985. Similarly, the time trend coefficient has also increased and it
120 becomes statistically significant during the last years of the sample. Other studies have
121 also investigated the time trends in climatological data with shorter time series,
122 including among others the works by Gil-Alana (2003) on the CET; Caballero et al.
123 (2002) for the multidecadal daily time series from CET, Chicago and Los Angeles; Gil-
124 Alana (2010), for the monthly data in specific locations in Spain and Portugal; Franzke
125 (2012) in four stations: central England; Stockholm (Sweden); Faraday-Vernadsky
126 (Antarctic Peninsula) and Alert (Canada); Percival et al. (2001) and Gil-Alana (2012),
127 for monthly temperatures in Alaska; Kane & Usman (2013) for the Sokoto metropolis in
128 Nigeria, or Franzke (2010), Bunde et al. (2014), and Ludescher et al. (2016), for
129 monthly temperatures of different stations of Antarctica.

130

131 **2. The model**

132 Let us suppose that y_t is the time series we observe, in our case, the European average
 133 temperature anomalies, and, in order to test for a climate warming over time, we
 134 consider the following (linear) model,

$$135 \quad y_t = \beta_0 + \beta_1 t + x_t; \quad t = 0, 1, \dots, \quad (1)$$

136 where β_0 and β_1 are unknown coefficients referring respectively to the intercept and the
 137 time trend. Thus, β_1 measures the mean change in the temperatures by unit time (in our
 138 case, years), and, in order to test for warming, we can test the null hypothesis:

$$139 \quad H_0 = \beta_1 = 0, \quad (2)$$

140 against the one-sided alternative: $\beta_1 > 0$. However, instead of assuming as in the
 141 standard cases, that the detrended process x_t in (1) is I(0) stationary, or alternatively,
 142 I(1) nonstationary, we estimate its order of integration from the data by means of the
 143 following model,

$$144 \quad (1 - B)^d x_t = u_t, \quad t = 0, \pm 1, \dots, \quad (3)$$

145 where B refers to the backshift operator, i.e., $Bx_t = x_{t-1}$, d can be any integer or
 146 fractional value, and u_t is assumed to be I(0). Related with this latter component (u_t), we
 147 will suppose first that u_t in (3) is uncorrelated (white noise, i.e. $u_t = \varepsilon_t$); however, weak
 148 autocorrelation will also be permitted by using an autoregression of order 1 (AR(1), i.e.,
 149 $u_t = \rho u_{t-1} + \varepsilon_t$) process, but also by using a non-parametric specification due to
 150 Bloomfield (1973), which approximates highly parameterized ARMA processes with
 151 very few parameters. (See Gil-Alana 2004 for a complete description of this model in
 152 the context of fractional integration). The estimation is carried out using the Whittle
 153 function in the frequency domain (Dahlhaus 1989, Robinson 1994 and others).

154

155 **3. Data**

156 We use the data collected by Mariani & Zavatti (2017), referring to the European
157 average temperature anomalies for the time period 1655 – 2017. According to these
158 authors, it was from the start of this period that the idea of spreading meteorological
159 instruments at a European level to promote an observational network able to operate in a
160 coordinated manner flourished for the first time (Iafrate 2008). The 29 data stations
161 (reported in the Appendix) were chosen with the aim of organizing an easily updatable
162 dataset which allows us to give an overview of the trend of European climate over the
163 long time periods covered by instrumental data. In order to obtain a representative area
164 average, the data of each station were converted into anomalies with respect to the
165 average temperature 1961-1990 of the station itself. The final dataset, displayed in
166 Figure 1, is the yearly average European temperature anomaly for the period 1655-2017,
167 and it is available at: “[http://www.climatemonitor.it/wp](http://www.climatemonitor.it/wp-content/uploads/2018/03/EUROPA_TD_da_1655_DATI-E-risultati.xls)
168 [-content/uploads/2018/03/EUROPA_TD_da_1655_DATI-E-risultati.xls](http://www.climatemonitor.it/wp-content/uploads/2018/03/EUROPA_TD_da_1655_DATI-E-risultati.xls)”

169 **[Insert Figure 1 about here]**

170 As a final remark here is important to note that these temperature series
171 proposed in Mariani & Zavatti (2017) are negatively affected by changes in
172 measurement units, observational standards (e.g., time of observation), location of
173 instruments and by the intensity of urban effects (intensity of the urban heat island,
174 UHI). Thus, results presented below should be taken with a bit of caution.

175

176 **4. Results**

177 We display in Table 1 the estimated coefficients in the model given by

$$178 \quad y_t = \beta_0 + \beta_1 t + x_t, \quad (1 - B)^d x_t = u_t, \quad t = 1, 2, \dots, \quad (4)$$

179 under the three assumptions of uncorrelated, AR(1) and Bloomfield-type errors. As
180 mentioned above the approach in Bloomfield (1973) is non-parametric in the sense that

181 no explicit model is presented for u_t , and it is exclusively specified in terms of its
182 spectral density function, which is given by:

$$183 \quad f(\lambda; \sigma^2) = \frac{\sigma^2}{2\pi} \exp\left(2 \sum_{r=1}^m \tau_r \cos(\lambda r)\right), \quad (5)$$

184 where σ^2 is the variance of the error term, λ refers to the frequency constrained between
185 0 and π , and m indicates the last of the Fourier frequencies which is associated with the
186 short run parameters. Bloomfield (1973) showed that the above equation can
187 approximate extremely well the spectral density of any highly parameterized ARMA,
188 since this model also produces autocorrelations decaying exponentially fast, and Gil-
189 Alana (2004, 2008a) showed that this model is very suitable in the context of fractional
190 integration, and more in particular with the version of the tests of Robinson (1994) used
191 in this work; moreover, this model is stationary across all values of τ unlike what
192 happens in the ARMA case.²

193 The first thing we observe in Table 1 is that the estimated value of d is found to
194 be significantly positive in the three cases, being around 0.3 under no autocorrelation,
195 and slightly higher (about 0.4) with autocorrelated disturbances. This is consistent with
196 many other studies also reporting evidence of long memory in temperatures, e.g., Gil-
197 Alana (2003), Lennartz & Bunde (2009), Rea et al. (2011), Bunde (2017), etc. On the
198 other hand, the time trend coefficient is statistically positive in the three cases: 0.0029
199 with white noise errors, and 0.0028 with autocorrelation, being these values slightly
200 higher than the one obtained under the assumption of $I(0)$ errors (i.e., $d = 0$ in (4))
201 (0.0027). Figure 1 also displays the estimated time trend (for the autocorrelated model)
202 along with the observed data.

² Alternatively, we could have used ARFIMA(p, d, q) models (Beran, 1995); however, in this context, we need to be extremely cautious about the orders p and q for the short run dynamics since misspecification of these components lead to an inconsistent estimate of the differencing parameter d .

203 We next examine the stability of the two parameters (persistence and time trend
204 coefficient) across the sample period, and for this purpose we use recursive estimation
205 of the parameters, starting with a subsample from 1655 to 1900, adding then
206 successively five observations each time till completing the whole sample. That is, we
207 consider again the model in (4), estimating the parameters β_0 , β_1 and d , first for a
208 subsample ending at 1900, and then, re-estimating the parameters adding five
209 observations each time. The results in terms of the estimates of d (persistence) and β_1
210 (time trend) are displayed in Figure 2.

211 **[Insert Figure 2 about here]**

212 Starting with the degree of persistence, in the upper part of the figure, we
213 observe that the estimate of the fractional differencing parameter has remained
214 relatively stable during most subsamples, observing a slight increase especially when
215 we incorporate data from 1985 onwards. This indicates that temperatures have become
216 gradually more persistent, especially during the last years in the sample. Focusing on
217 the time trend coefficient (lower part of Figure 2) we notice that the time trend has been
218 successively increasing across the different subsamples, though it has become
219 statistically significantly positive only during the last four subsamples, that is,
220 incorporating the data from 2010 onwards.

221 **[Insert Table 2 about here]**

222 Table 2 reports the estimates of the differencing parameter and the time trend
223 coefficient for the last 18 subsamples, starting from 2000. Both coefficients have
224 increased across the subsamples, from 0.35 to 0.41 in case of the persistence parameter,
225 and from 0.0019 to 0.0028 in case of the time trend coefficient. This last result indicates
226 that the increase in the temperatures has become particularly relevant during the last ten

227 years of the sample suggesting the relevance of the last period of the sample in the
228 analysis of the global warming.

229 As a robustness method and in order to check if the beginning of the series has
230 produced changes due to the artificial long term variability, we repeat the analysis of
231 four different subsamples, the first three with 100 observations each (1655 – 1754; 1755
232 – 1854, and 1855 – 1954), and the final one with the last 62 observations (1955 – 2017).
233 We estimate d for the three potential set-ups for the error term: white noise, AR(1) and
234 Bloomfield-type disturbances, and the results are displayed in Table 3. We observe that
235 if u_t is white noise, long memory takes place in the first two subsamples, but short
236 memory (or $I(0)$ behaviour) is found in the remaining two. The same happens under the
237 exponential model of Bloomfield, and if u_t is AR(1), long memory only takes place
238 during the first subsample. Focussing on the time trends, the coefficients are statistical
239 significant in the last two subsamples in the three cases.

240

241 **5. Discussion**

242 Two features have been examined in this work in relation with the European
243 temperatures: the degree of persistence in the data and the existence of time trends.
244 Dealing with the first of these two issues, our results show evidence of long memory
245 patterns in the temperatures, since the order of integration of the series is found to be
246 significantly positive. This is consistent with other studies that find the same patten in
247 global (Gil-Alana, 2005, 2008b; Hare and Mantua, 2000; Ivanov and Evtimov, 2010,
248 Coggin, 2012; etc.) but also at specific locations all over the world (Caballero et al,
249 2002; Gil-Alana, 2003; Franzke, 2010; Bunde et al, 2014; Ludescher et al, 2016; etc.).

250 The fact that long memory is present in the data has also important implications
251 for the estimation of the time trend. Thus, ignoring this feature produces bias in the

252 estimate of the time trend coefficient reducing its magnitude and thus reducing the
253 increase in the temperatures. Our results indicate that the European average
254 temperatures increase about 0.2°C every 100 years though this coefficient is slightly
255 higher if we only consider data from the most recent past.

256

257 **6. Concluding comments**

258 We have examined in this work the persistence and the time trend in the European
259 average temperature anomalies for the period from 1655 to 2017 using a new dataset
260 gathered by Mariani & Zavtti (2017) and based on the information provided by 29
261 European stations. The results indicate that long memory is present in the data, with an
262 order of integration in the stationary range (0, 0.5). On the other hand, the time trend
263 coefficient is significantly positive, though using recursive estimation methods, we
264 show that the significance in this parameter becomes relevant (statistically significant)
265 when incorporating only the data from 2010 onwards. Separating the overall data in
266 four subsamples, (the first three with 100 observations and the last one with the last 62
267 observations) we obtain evidence of long memory only during the first subsamples,
268 which may be related with a potential artificial long term variability, and the time trend
269 coefficients are only significant during the last two subsamples. Thus, these results
270 provide further evidence supporting the increase in the temperatures in Europe in recent
271 years.

272 With respect to the long memory property, this feature is observed when using
273 the whole sample period, and it is consistent with many other works on climatological
274 data (Percival et al. 2001; Gil-Alana, 2003, 2005, 2010; 2017; Lennartz & Bunde
275 (2009), Rea et al. (2011), Franzke (2012), Yuan et al. (2013, 2015), Bunde et al.,
276 (2014), Ludescher et al. (2016), Bunde (2017), etc.). The fact that this property is not

277 observed in some of the subsamples is clearly due to the wide confident intervals
278 associated to the smaller sample sizes.

279 A drawback of the resent work is that it is based on raw observations and
280 therefore potentially affected by changes in measurement conditions which may
281 produces biases in the estimation of both the time trend coefficient and the fractional
282 differencing parameter (see, e.g., Rust, Mestre & Venema, 2008). In this respect, the use
283 of homogenization can solve this problem by comparing for example the results using
284 both raw and homogenized data. In addition, the use of structural breaks and recursive
285 estimation methods may also be helpful. Work in this direction is now in progress.

286

288 **Appendix: List of the 29 stations**

	Acronym	Latitude	Longitude
Central England Temperatures	CET	-1.00	52.00
Sonnblick	SBLI	12.95	47.05
Hamburg Fuhlsbuttel	HAMB	9.59	53.38
Navacerrada	NAVA	-3.59	40.46
Salamanca	SALA	-5.28	40.56
Bourges	BOUR	2.37	47.07
Mont-Aigoual	MAIG	3.35	44.07
Rennes Renn	RENN	1.44	48.04
Strasbourg	STRB	7.63	48.55
Toulouse (Blagnac)	TOUL	1.22	43.37
Uppsala	UPPS	17.38	59.51
Stockholm	STOC	18.04	59.19
Berlin Tempelhof	BERL	13.24	52.31
Paris Montsouris	PARI	2.34	48.82
St. Petersburg	SPIE	30.19	59.56
Frankfurt Am	FFUR	8.41	50.07
Kremsmuenster	KREM	14.08	48.03
CBT_Belgium-Bruxelles	BRUX	4.60	50.51
De-Bilt	DEBI	5.18	52.10
Poprad Tatry	POPR	20.25	49.07
Waddington (Lincoln)	WDD	0.52	53.17
Basel-Binningen	BASL	7.60	47.60
Verona Villafranca	VERO	10.52	45.23
Cagliari Elmas	CAGL	9.13	39.14
Brindisi	BRIN	17.56	40.38
Padova	PADO	11.52	45.24
Cadiz	CADI	-6.17	36.31
Col du Gran St_Bernard	CGSB	7.17	45.87
Florence	FIRE	11.20	43.81

291

292 **References**

293

294 Andronova N, Schlesinger M (2000) Causes of global temperature changes during the
295 19th and 20th centuries. *Geophys Res Lett* 27:2137-2140

296

297 Beran, J. (1994) *Statistics for Long-Memory Processes*. Chapman & Hall, New York.

298 Bloomfield P (1973) An exponential model in the spectrum of a scalar time series.
299 *Biometrika* 60:217–226

300

301 Bunde A (2017) Long-term memory in climate: Detection, extreme events and
302 significance of trends. Chapter 11 in *Nonlinear and Stochastic Climate Dynamics*,
303 edited by Christian L.E. Franzke and Terence O’Kane, Cambridge University Press.

304

305 Bunde A, Ludescher J, Franzke CLE, Büntgen U (2014) How significant is West
306 Antarctic warming. *Nat Geosci* 7:246–247

307

308 Caballero R, Jewson S, Brix A (2002) Long memory in surface air temperature:
309 detection, modeling, and application to weather derivative valuation. *Clim Res* 21:127-
310 140

311

312 Camuffo D, Bertolin C (2012) The earliest temperature observations in the world. The
313 Medici Network (1654-1670). *Clim Change* 111:335-363

314

315 Camuffo D, Jones PD (2002) *Improved understanding of Past Climatic Variability from
316 Early Daily European Instrumental Sources*, Kluwer Academic Publisher.

317

318 Coggin TD (2012) Using econometric methods to test for trends in the HadCRUT3
319 global and hemispheric data. *Int J Climatol* 32:315–320.

320

321 Dahlhaus R (1989) Efficient parameter estimation for self-similar process. *Ann Stat* 17:
322 1749-1766

323

324 Franzke C (2010) Long-range dependence and climate noise characteristics of Antarctic
325 temperature data. *J Clim* 23:6074–6081

326

327 Franzke C (2012) Nonlinear trends, long-range dependence, and climate noise
328 properties of surface temperature. *J Clim* 25:4172–4183.

329

330 Gil-Alana LA (2003) An application of fractional integration to a long temperature time
331 series. *Int J Climatol* 23:1699–1710

332

333 Gil-Alana LA (2004) The use of Bloomfield (1973) model as an approximation to
334 ARMA processes in the context of fractional integration. *Math Comput Model* 39:429-
335 436

336

337 Gil-Alana LA (2005) Statistical model for the temperatures in the Northern hemisphere
338 using fractional integration techniques. *J Clim* 18:5537–5369

339

340 Gil-Alana, L.A. (2008a), Fractional integration with Bloomfield exponential spectral
341 disturbances. A Montecarlo experiment with an application, *Brazilian Journal of*
342 *Probability and Statistics* 22, 1, 69-83.
343

344 Gil-Alana, LA (2008b) Time trend estimation with breaks in temperature time series,
345 *Clim Change* 89:325–337.
346

347 Gil-Alana LA (2010) Climate change in the Iberian Peninsula. Evidence based on
348 fractional integration techniques. *Seguridad y Medio Ambiente* 117:50-62
349

350 Gil-Alana LA (2012) Long memory, seasonality and time trends in the average monthly
351 temperatures in Alaska. *Theor Appl Climatol* 108:385–396, doi: 10.1007/s00704-011-
352 0539-0
353

354 Gil-Alana LA (2017) Alternative modelling approaches for the ENSO time series.
355 Persistence and seasonality. *Int J Climatol* 37:2354–2363
356

357 Hare SR, Mantua NJ (2000) Empirical evidence for North Pacific regime shifts in 1977
358 and 1989. *Progr Oceanogr* 47:103–145.
359

360 Iafrate L (2008) *Fede e Scienza: un incontro proficuo. Origini e sviluppo della*
361 *meteorologia fino agli inizi del 900.* Roma: Ateneo Pontificio Regina Apostolorum
362 (Scienza e Fede), Saggi
363

364 Ivanov MA, Evtimov SN (2010). 1963: The break point of the Northern Hemisphere
365 temperature trend during the twentieth century, *Int J Climatol* 30:1738–1746.
366

367 Klein AMG, Können GP (2003) Trends in Indices of Daily Temperature and
368 Precipitation Extremes in Europe, 1946–99. *J Clim* 16:3665-3680
369

370 Kaufmann R, Kauppi H, Mann M, Stock J (2011) Reconciling anthropogenic climate
371 change with observed temperature 1998-2008. *Science* 108:11790-11793,
372 <https://doi.org/10.1073/pnas.1102467108>
373

374 Lennartz S, Bunde A (2009) Trend evaluation in records with long-term memory:
375 Application to global warming. *Geophys Res Lett* 36:L16706, doi:
376 10.1029/2009GL039516

377 Løvsletten, O., Rypdal, M (2016) tatistics of Regional Surface Temperatures after 1900:
378 Long-Range versus Short-Range Dependence and Significance of Warming Trends. *J*
379 *Clim* **:

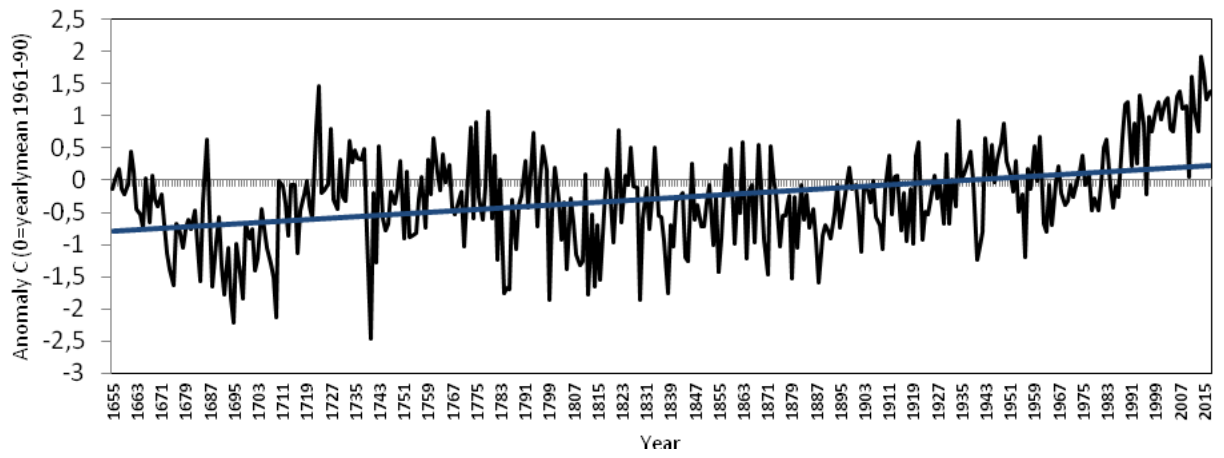
380 Ludescher J, Bunde A, Franzke CL, Schellnhuber HJ (2016). Long-term persistence
381 enhances uncertainty about anthropogenic warming of Antarctica. *Clim Dyn* 46:263–
382 271, doi: 10.1007/s00382-015-2582-5
383

384 Luterbacher J, Dietrich D, Xoplaki M, Wanner H (2004). European Seasonal and
385 Annual Temperature Variability, Trends, and Extremes Since 1500. *Science* 303:1499-
386 1503
387

388 Mariani L, Zavatti F (2017) Multi-scale approach to Euro-Atlantic climatic cycles based
389 on pehnological time series air temperatures and circulation indexes. *Science of the*
390 *Total Environment* 593-594:253-262
391
392 MetOffice _ Hadley Centre, 2015, Hadley Centre, Central England Temperature,
393 HadCET database. <https://www.metoffice.gov.uk/hadobs/hadcet/> (visited at 23/07/2018)
394
395 Myrvoll-Nilsen, E., Sørbye, S. H., Rue, H. (2017). An approximate fractional Gaussian
396 noise model with linear computational complexity. Manuscript in progress.
397
398 Moberg A, Jones PD (2005) Trends in índices por extremes in daily temperatura and
399 precipitation in central and western Europe, 1901-99. *Int J Climatol* 25:1149-1171
400
401 Percival DB, Overland JE, Mofjeld HO (2001) Interpretation of North Pacific
402 variability as a short- and long-memory process. *J Clim* 14:4545-4559
403
404 Philipona R, Behrens K, Ruckstuh C (2009)How declining aerosols and rising
405 greenhouse gases forced rapid warming in Europe since the 1980s. *Geophys Res Lett*
406 36, <https://doi.org/10.1029/2008GL036350>
407
408 Rea W, Reale M, Brown J (2011) Long memory in temperature reconstruction, *Clim*
409 *Change* 107:247-265
410
411 Rimfrost, 2016 Data on global weather stations. <http://www.rimfrost.no/>
412
413 Robinson PM (1994) Efficient tests of nonstationary hypotheses. *J Am Stat Assoc*
414 89:1420-1437
415
416 Rust HW, Mestre O, Venema, VKC (2008) Fewer jumps, less memory: Homogenized
417 temperature records and long memory. *J Geophys Res* 113:D19110
418
419 Yuan N, Fu Z, Liu S (2013) Long-term memory in climate variability: A new look
420 based on fractional integral techniques. *J Geophys Res Atmos* 118:962-969
421
422 Yuan N, Ding M, Huang Y, Fu Z, Xoplaki E, Luterbacher J (2015) On the long-term
423 climate memory in the surface air temperature records over Antarctica: A non-
424 negligible factor for trend evaluation. *J Clim* 28:5922-5934.
425
426 Zhou, L, Dai, A, Dai, Y, Vose, RS, Zou, C, Tian, Y, Chen, H (2009) Spatial dependence
427 of diurnal temperature range trends on precipitation from 1950 to 2004. *Clim Dyn*
428 32:429-440
429
430

431

432



433

434

435

Figure 1: European average temperature anomalies and its estimated trend

436

437

438

439

440 **Table 1: Estimated coefficients in the selected models**

	d (95% band)	Intercept	Time trend	Autocorrelation
White noise	0.30 (0.25, 0.36)	-0.6739 (0.002)	0.0029 (0.002)	----
AR(1)	0.40 (0.32, 0.49)	-0.5584 (0.069)	0.0028 (0.034)	-0.178
Bloomfield	0.41 (0.33, 0.53)	-0.5448 (0.082)	0.0028 (0.038)	-0.190

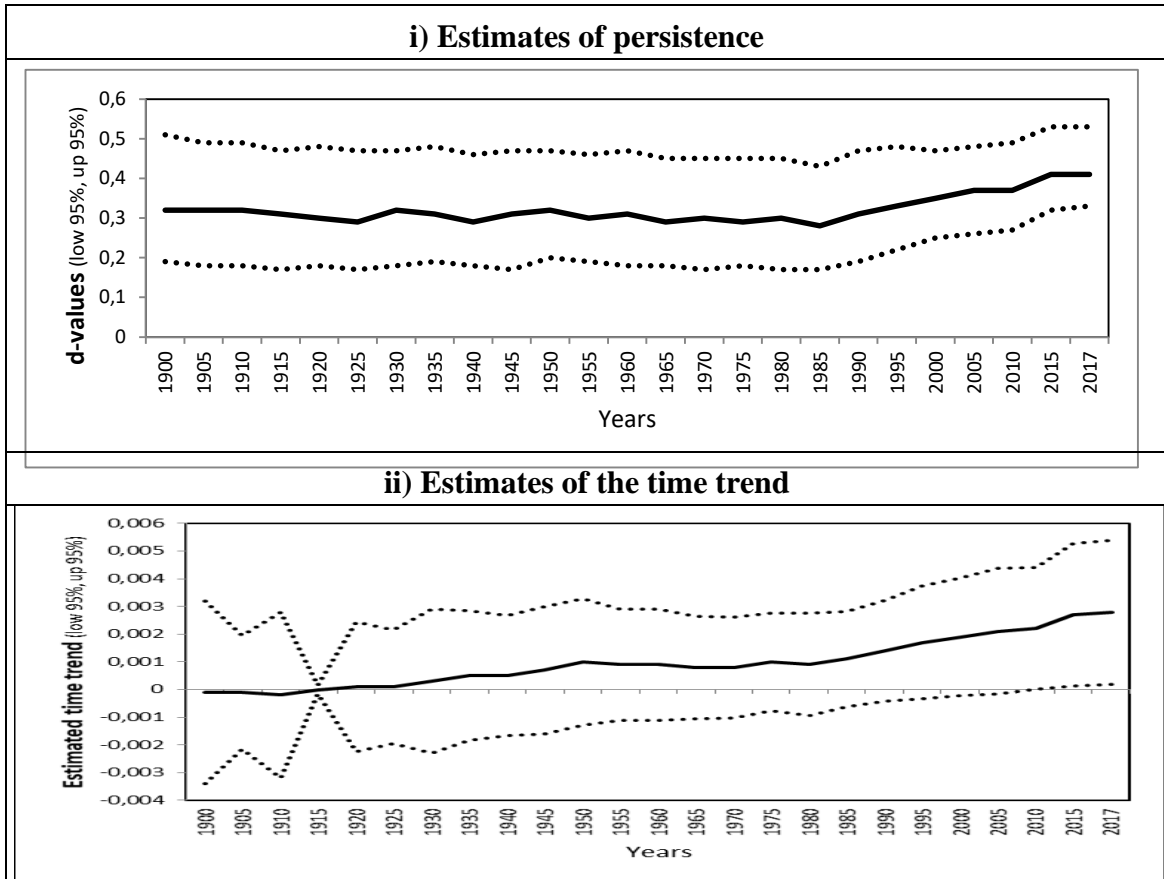
441 The values in parenthesis in the 3rd and 4th columns refer to the corresponding p-values.

442

443

444

445



447 **Figure 2: Persistence and trend recursive coefficients**

448

449

450

451

452

453
 454
 455

Table 2: Estimated coefficients for persistence and trend from 2000 onwards

Sample period	Persistence d (95% band)	Time trend β_1 (p-value)
1655 – 2000	0.35 (0.25, 0.47)	0.0019 (0.071)
1655 – 2001	0.35 (0.25, 0.47)	0.0019 (0.067)
1655 – 2002	0.37 (0.27, 0.49)	0.0020 (0.075)
1655 – 2003	0.38 (0.26, 0.50)	0.0021 (0.073)
1655 – 2004	0.37 (0.28, 0.49)	0.0021 (0.065)
1655 – 2005	0.37 (0.26, 0.48)	0.0021 (0.064)
1655 – 2006	0.38 (0.27, 0.50)	0.0022 (0.062)
1655 – 2007	0.38 (0.29, 0.52)	0.0023 (0.054)
1655 – 2008	0.38 (0.29, 0.51)	0.0023 (0.051)
1655 – 2009	0.39 (0.30, 0.51)	0.0024 (0.054)
1655 – 2010	0.37 (0.27, 0.49)	0.0022 (0.049)
1655 – 2011	0.39 (0.29, 0.50)	0.0024 (0.049)
1655 – 2012	0.39 (0.29, 0.50)	0.0024 (0.047)
1655 – 2013	0.39 (0.30, 0.50)	0.0024 (0.048)
1655 – 2014	0.40 (0.31, 0.52)	0.0026 (0.042)
1655 – 2015	0.41 (0.32, 0.53)	0.0027 (0.043)
1655 – 2016	0.40 (0.32, 0.52)	0.0027 (0.036)
1655 – 2017	0.41 (0.33, 0.53)	0.0028 (0.038)

456 In bold, the significant time trend coefficients at the 5% level.

457
 458
 459
 460
 461
 462

464 **Table 3: Estimated coefficients in the selected models**

i) White noise				
	d (95% band)	Intercept	Time trend	Autocorrelation
1 st subsample	0.35 (0.25, 0.49)	-0.4257 (0.084)	----	----
2 nd subsample	0.14 (0.03, 0.28)	-0.4155 (0.000)	----	----
3 rd subsample	0.03 (-0.09, 0.20)	-0.6323 (0.000)	0.0064 (0.000)	----
4 rd subsample	0.05 (-0.10, 0.29)	-0.5389 (0.000)	0.0299 (0.000)	----
ii) AR(1)				
	d (95% band)	Intercept	Time trend	Autocorrelation
1 st subsample	0.32 (0.18, 0.50)	-0.4426 (0.046)	----	0.042
2 nd subsample	0.26 (-0.07, 0.53)	-0.4029 (0.032)	----	-0.171
3 rd subsample	0.00 (-0.31, 0.34)	-0.6337 (0.000)	0.0064 (0.000)	0.038
4 rd subsample	-0.17 (-0.33, 0.36)	-0.5609 (0.000)	0.0302 (0.000)	0.275
iii) Bloomfield				
	d (95% band)	Intercept	Time trend	Autocorrelation
1 st subsample	0.33 (0.14, 0.57)	-0.4372 (0.056)	----	0.029
2 nd subsample	0.25 (0.03, 0.67)	-0.4039 (0.023)	----	-0.170
3 rd subsample	-0.01 (-0.19, 0.23)	-0.6342 (0.000)	0.0064 (0.000)	0.059
4 rd subsample	-0.07 (-0.32, 0.30)	-0.5536 (0.000)	0.0301 (0.000)	0.160

465 The values in parenthesis in the 3rd and 4th columns refer to the corresponding p-values