

1 **Modelling of the anaerobic semi-continuous co-digestion of sewage sludge and**
2 **wine distillery wastewater.**

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4 Vanessa Ripoll^{a, b}

5 Cristina Agabo-García^a

6 Rosario Solera^a

7 Montserrat Pérez^{a, *}

8 ***Author to whom correspondence will be addressed**

9

10 **Affiliation**

11 ^a Department of Environmental Technologies, University of Cadiz, Campus de Puerto
12 Real, 11500 Puerto Real, Cadiz, Spain.

13 ^b Current affiliation: Facultad de Ciencias Experimentales, Universidad Francisco de
14 Vitoria (UFV), Ctra. Pozuelo-Majadahonda km 1.800, 28223 Pozuelo de Alarcón,
15 Madrid, Spain

16

17 **E-mail addresses**

18 vanessa.ripoll@ufv.es (V. Ripoll)

19 crisrina.agabo@uca.es (C. Agabo)

20 rosario.solera@uca.es (R. Solera)

21 montserrat.perez@uca.es (M. Pérez)

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24 **ABSTRACT**

25 The semi-continuous mesophilic anaerobic co-digestion of sewage sludge and wine
26 distillery wastewater was investigated. In this sense, the effects of reducing hydraulic
27 retention time (HRT, from 20 d to 8 d) on the degradation of organic matter and
28 methane production were determined. The experimental results showed that anaerobic
29 co-digestion enhanced the biodegradability of the mixture in terms of VS and CODt (7-
30 8% higher) for HRT = 8 d. The methane productivity at HRT = 8 d ($18.0 \text{ L}_{\text{CH}_4}/\text{kg}_{\text{VS}} \cdot \text{d}$),
31 was also enhanced (30% higher) than those obtained in the control experiment. In
32 addition, a mathematical kinetic model was proposed to determine the rate-limiting step
33 of the process. Stoichiometric parameters obtained for SS:WDW ($0.115 \text{ kg}_{\text{CH}_4}/\text{kg}_{\text{COD}}$)
34 was higher than SS ($0.094 \text{ kg}_{\text{CH}_4}/\text{kg}_{\text{COD}}$), which means that co-digestion increased the
35 rate of consumption because more amount of biodegradable compounds. Kinetic study
36 showed that anaerobic co-digestion favoured methane production rate enhancing the
37 acetate consumption step and making methanogenesis the rate-limiting step in this
38 process.

39 **Keywords:** *anaerobic co-digestion; wine distillery wastewater; sewage sludge; organic*
40 *loading rate; kinetic modelling.*

41

42 **1 Introduction**

43 The cost of sewage sludge management in urban wastewater treatments plants (WWTP)
44 is over 50% of the overall operating costs taking into account the land value, the
45 transportation, landfilling operation and leachate treatment, and maintenance for a
46 correct pollution control¹. Therefore, anaerobic digestion (AD) has been widely
47 implemented as an effective technology at an industrial scale in WWTP². AD is a

48 renewable energy technology in which microorganisms break down biodegradable
49 material in an oxygen-free environment to produce a solid digestate along with biogas.
50 Biogas production has social advantages, such as the economical production of
51 electricity or heat. In addition, AD process achieves the reduction and stabilization of
52 rotting organic matter and partial inactivation of pathogenic agents³⁻⁵. However, sewage
53 sludge (SS) organic load values undergo high variations and are often not sufficient for
54 an economically effective operation¹. Given that many of the anaerobic digesters
55 installed in WWTP are oversized, the scientific community is paying close attention to
56 simultaneous anaerobic co-digestion (ACoD) of SS and other types of waste aimed to
57 promote the biodegradability of the feedstock and hence to enhance biogas production⁶
58 ⁷. The main advantages of ACoD include: shared treatment facilities, reduced
59 investment and operating costs, buffering of the variations in the composition of the
60 waste over time and the diluting of toxic compounds and cytotoxic inhibitors. Several
61 published studies have already focused on the employment of agro-industrial wastes,
62 which contain easily degradable substrates⁸⁻¹¹. Among different residues, wine distillery
63 wastewater (WDW) is one of the main types of waste generated in the viticulture
64 industry and its disposal constitutes an environmental concern. This waste has a
65 strongly acidic pH and contains a high organic pollutant load (around 40 gCOD/L)
66 including various phenolic compounds such as gallic acid, p-coumaric acid and gentisic
67 acid¹². In this sense, the AD of sole WDW at semi-continuous mode has been previously
68 studied (including kinetic evaluation) as a successful biological treatment for producing
69 biomethane: in fixed-film reactors¹³; thermophilic high rate reactors ¹⁴ and after
70 different pre-treatments¹⁵. However, semi-continuous ACoD of SS:WDW only has been
71 previously studied to produce biohydrogen at thermophilic conditions in continuous
72 stirred tank reactor technology (CSTR)¹⁶. In addition, the ACoD of SS:WDW has been

73 previously studied at batch mode without any pretreatment¹⁷. So, in the present work it
74 was studied its biomethane potential as co-substrate for continuous biomethane
75 production in CSTR technology and the kinetic parameters, complementing the recently
76 research published about ACoD of SS:WDW at batch mode. This information will be
77 useful for determining operational conditions in scaling-up process in regions with high
78 volume of WDW production in order to use them in WWTP in wine-producing areas¹⁷.

79

80 In this sense, process modelling is a useful tool for describing and predicting the
81 performance of anaerobic digestion systems. Monod type kinetic models have been
82 widely used to describe the process kinetics of anaerobic digesters¹⁸. Although there has
83 been some success in applying Monod type kinetics to the anaerobic process, some
84 research workers found it difficult to apply them for their systems¹⁹⁻²⁰. In the equation
85 proposed by Contois (1959)²¹, the specific growth rate was considered as a function of
86 the growth-limiting nutrient in both input and effluent substrate concentration by using
87 an empirical constant, which was related to microbial concentration. On this basis, Chen
88 and Hashimoto (1980)²² developed kinetic models for substrate utilisation and methane
89 production and suggested that the Contois type kinetic models would be more suitable
90 than the Monod type kinetic models to predict digester performance. Both consider that
91 the AD takes place throughout a single stage of biological reaction that combines a
92 complex biological reaction network. In this paper, a novel kinetic model is proposed
93 based on the methane production results to describe the step rates involved in the
94 anaerobic process. An unstructured non-segregated kinetic model is proposed to
95 describe the anaerobic digestion considering two steps: the hydrolysis of the particulate
96 substrate (COD_P) to obtain accessible or soluble substrate (COD_S) for the
97 microorganisms and the consumption of this accessible substrate to produce methane.

98 Moreover, there is not much published information available for the process kinetics of
99 anaerobic co-digestion treating sewage sludge and wine distillery wastewater.

100

101 The aim of this paper was focused, therefore, on the experimental and kinetic
102 description of the anaerobic semi-continuous co-digestion of SS and WDW within the
103 mesophilic temperature range, studying the influence of the organic loading rate (OLR)
104 on the overall process: the efficiency of organic matter removal, biogas production and
105 kinetic analysis. In order to achieve this goal, several hydraulic retention times (HRT)
106 were employed ranging from 20 to 8 d, corresponding to different OLR ranges (2.26 –
107 5.38 kgCOD/m³·d). An anaerobic digestion trial using only sewage sludge as feedstock
108 was also carried out as a control experiment to determine whether adding WDW to the
109 WWTP anaerobic digester enhances the degradation of organic matter and/or methane
110 production. The semi-continuous control experiment was carried out under the same
111 HRT conditions (from 20 to 8 d), involving an OLR range from 3.43 to 6.99
112 kgCOD/m³·d. Finally, a comparison of different kinetic parameters obtained after
113 modelling was made to determine the rate-limiting step in each case.

114

115 **2 Materials and methods**

116 The experimental protocol was designed to study the influence of increasing OLR on
117 the efficiency of an anaerobic digestion treatment within the mesophilic temperature
118 range employing a 1:1 (v/v) ratio of SS:WDW, as well as SS alone (as a control
119 experiment).

120

121 The methods and materials used are briefly described in this section. Each trial was
122 carried out in duplicate and all the reported results correspond to the average values of
123 the last data obtained.

124 **2.1 Feedstock and inoculum**

125 The substrates used in the experimental stage were collected directly from two real
126 industrial facilities. SS corresponds to the activated sludge from the secondary treatment
127 employed at Guadalete municipal WWTP (located in Cadiz, Spain). WDW was
128 obtained from Gonzalez-Byass, an ethanol producing wine-distillery plant located in
129 Jerez de la Frontera (Cadiz, Spain). All the samples were characterized on reception at
130 the laboratory and were stored at 4 °C for a maximum of one month before being used
131 in the experiments in order to prevent their degradation.

132

133 The experimental work was carried out over a period of 6 months. During the
134 experiments, waste samples had to be collected several times. Parameters related to
135 organic material content, such as total solids (TS), volatile solids (VS) and chemical
136 oxygen demand (COD), were determined.

137 The inoculum was obtained from a 5-L laboratory scale anaerobic digester operating the
138 Research Group under stable conditions at 20 d HRT within the mesophilic temperature
139 range (35 °C). This reactor was fed with SS coming from secondary decanter of WWTP
140 from Jerez (Cádiz-Spain). The characteristics of the inoculum are shown in Table 1.

Table 1. Characteristics of inoculum

Parameters	Inoculum
pH	7.60 ± 0.02
CODt (kg/m ³)	20.1 ± 0.5

CODs (kg/m ³)	10.1 ± 0.4
TS (g/L)	32.0 ± 2.5
VS (g/L)	23.4 ± 2.0

141

142 **2.2 *Experimental equipment***

143 A 3-L semi-continuous stirred tank reactor with a working volume of 2-L was used
144 (MiniReactor, Trallero and Schee®) in this study. The digester was sealed with a lid
145 provided with several openings for different purposes (biogas output, pH probe,
146 temperature probe, stirring system). The stirring speed was set at 20 rpm. The
147 temperature was maintained within the mesophilic range (35 ± 1 °C) by means of an
148 electric heater. The produced biogas was collected in 5-L Tedlar® bags, employing a
149 special syringe to sample the gases.

150

151 **2.3 *Operating conditions***

152 In the present study, the influence of the OLR on the anaerobic co-digestion of a 1:1
153 (v/v) mixture of SS and WDW was analysed in semi-continuous operating mode within
154 the mesophilic temperature range (35 °C). These results were compared with the
155 behaviour of an anaerobic digester using only SS working under similar operating
156 conditions (OLR and temperature range). Initially, both digesters were loaded with a
157 mixture of inoculum and substrate at a ratio of 1:2.5 (v/v), which is considered optimal
158 for biogas production^{17, 23}. The start-up of the reactors took place at 20 d HRT. The
159 subsequent series of HRT were set at 15, 10 and 8 days, which involved progressive
160 increases in feed flow rates (from 0.10 to 0.15, 0.2 and 0.25 L/d, respectively). These
161 operating conditions were selected on the basis of the previous experience of our

162 research group ^{8,10} and other research contributions ²⁴⁻²⁵. At least 3 trials employing the
 163 corresponding HRT (20, 15, 10 and 8 d, respectively) were conducted under each
 164 operating condition in order to ensure the steady state. The reactors were fed once a day
 165 with SS:WDW (1:1 (v/v)) and SS without the addition of nutrients in order to establish
 166 the semi-continuous process. Each HRT was maintained at least 3 times to ensure that
 167 steady-state conditions were reached. The composition of the industrial wastes
 168 employed varied during the experimental period. Therefore, the OLR was determined
 169 for each condition in terms of feed VS (OLR_{VS}) and feed COD (OLR_{COD}). The main
 170 characteristics of the feedstocks are shown in Table 2 (a, b).

Table 2. Main characteristic of the feedstock (a) 1:1 SS:WDW and (b) SS.

HRT (d)	TS (kg_{TS}/m^3)	VS (kg_{VS}/m^3)	COD _t (kg_{COD}/m^3)	COD _s (kg_{COD}/m^3)	OLR ($kg_{VS}/m^3 \cdot d$)	OLR ($kg_{COD}/m^3 \cdot d$)
20	30.6 ± 1.6	23.4 ± 0.8	45.2 ± 2.4	24.9 ± 1.7	1.17 ± 0.04	2.26 ± 0.12
15	31.7 ± 1.9	25.3 ± 1.1	43.0 ± 1.9	22.4 ± 1.3	1.90 ± 0.08	3.23 ± 0.14
10	31.8 ± 0.3	24.7 ± 0.4	41.9 ± 1.9	20.6 ± 2.2	2.47 ± 0.04	4.19 ± 0.19
8	34.7 ± 0.3	25.6 ± 0.4	43.0 ± 1.9	22.4 ± 1.3	3.20 ± 0.05	5.38 ± 0.24

171 (a)

HRT (d)	TS (kg_{TS}/m^3)	VS (kg_{VS}/m^3)	COD _t (kg_{COD}/m^3)	COD _s (kg_{COD}/m^3)	OLR ($kg_{VS}/m^3 \cdot d$)	OLR ($kg_{COD}/m^3 \cdot d$)
20	52.8 ± 2.0	43.2 ± 1.7	68.5 ± 3.3	15.9 ± 3.2	2.16 ± 0.09	3.43 ± 0.17
15	52.4 ± 0.4	42.6 ± 0.3	68.5 ± 2.0	10.4 ± 2.5	3.20 ± 0.02	4.57 ± 0.15
10	54.8 ± 0.3	42.9 ± 0.2	65.8 ± 3.3	9.9 ± 1.6	4.29 ± 0.02	6.58 ± 0.33
8	44.4 ± 0.5	37.8 ± 1.2	65.9 ± 0.8	10.4 ± 1.1	4.66 ± 0.15	6.99 ± 0.10

172

173 (b)

174 **2.4 Analytical methods**

175 Analytical characterization of the feedstock and the digestate were carried out twice a
176 week during the experimental stage. The main parameters (total solids (TS), volatile
177 solids (VS) and chemical oxygen demand (COD)) were determined in accordance with
178 the Standard Methods²⁶. In order to better understand the system behaviour, the total
179 and soluble COD (COD_T and COD_s, respectively) of both the feedstock and effluent
180 were determined. Volatile fatty acids (VFA) (acetic, propionic, iso-butyric, butyric, iso-
181 valeric, valeric, iso-caproic, caproic and heptanoic acids) were determined on a gas
182 chromatograph (GC-2010 Plus Shimadzu) employing a Nukol® capillary column and a
183 FID detector. Total acidity was calculated by the addition of the individual fatty acids in
184 terms of acetic acid concentration equivalent. Gas composition was determined
185 employing a gas chromatographic technique (GC-2010 Shimadzu). The analysed gases
186 (H₂, CH₄, CO₂, O₂ and N₂) were measured by means of a thermal conductivity detector
187 (TCD) at 250 °C using a Supelco Carboxen 1010 PLOT column. The oven temperature
188 was programmed between 35 and 200 °C. Manual injection was carried out using a
189 sample volume of 250 µL. The carrier gas employed was nitrogen at a pressure of 35
190 kPa. The biogas volume was collected daily in Tedlar bags. Volumes were directly
191 determined employing a gas flow meter (Ritter Wet Drum TG 0.1 mbar). The pH was
192 measured using a Crison 20 BASIC pHmeter.

193

194 **2.5 Process efficiency**

195 Process efficiency was related to the percent removal efficiency obtained by anaerobic
196 digestion in terms of VS removal and COD_T removal. In order to evaluate biogas

197 production, two parameters related to specific methane production (SMP) (Eq. 1 and 2)
198 and methane productivity (MP) (Eq. 3 and 4) were defined.

199

$$200 \quad SMP_{VS} \left(L_{CH_4} / kg_{VS} \right) = \frac{V_{CH_4}}{OLR_{VS}} \quad (1)$$

201

$$202 \quad SMP_{COD} \left(L_{CH_4} / kg_{COD} \right) = \frac{V_{CH_4}}{OLR_{COD}} \quad (2)$$

203

$$204 \quad MP_{VS} \left(L_{CH_4} / kg_{VS} \cdot d \right) = \frac{V_{CH_4}}{V_{Digester} \cdot VS_{INLET}} \quad (3)$$

205

$$206 \quad MP_{COD} \left(L_{CH_4} / kg_{COD} \cdot d \right) = \frac{V_{CH_4}}{V_{Digester} \cdot COD_{INLET}} \quad (4)$$

207

208 **3 Results and discussion**

209

210 **3.1 Process stability: pH evolution and VFA**

211 The evolution of pH inside the digesters throughout the experiments are shown in
212 Figure 1-A (i, ii). The optimal pH range for the activity of methanogenic
213 microorganisms (7.5–8.5) in mesophilic anaerobic digestion is well known²⁷⁻²⁹.

214

215 Thus, the monitoring of the physicochemical parameter provides useful information
216 with respect to the anaerobic digestion steps that are taking place. The pH values
217 remained within the 7.3–8.2 range in both the ACoD digester and the control
218 digester for months. The pH was maintained constant due to two causes: (i) daily

219 adjustment of substrate before feeding in the case of co-digestion (due to low values
220 of pH of WDW) and (ii) the microbial consortia activity. So, the pH was
221 maintained at optimal range and the volatile fatty acids, which are being formed
222 during hydrolytic-acidogenesis pathways, are neutralized avoiding acidification of
223 the reactor and allowing the normal activity of acetogenic and methanogenic
224 bacteria.

225

226 **3.2 Organic matter removal**

227 The organic matter content in the feedstock and effluent was determined by measuring
228 VS and COD_T in both streams. The evolution of these two key parameters during AD at
229 each tested HRT are shown in Figures 1-B (i, ii) and 1-C (i, ii) and the average of these
230 parameters after reaching steady state is showed in Table 2. As it can be seen in Figures
231 1B-C, the start-up of the process (20 d HRT) showed a proper acclimation of the
232 inoculum to the waste. The present study was conducted employing real industrial
233 wastes as feedstock. Thus, the characteristics of the initial feedstock varied over the six
234 months of experimental work. Nevertheless, the organic matter determined in the outlet
235 stream remained stable (Figure 1 B-C) regardless of the changes in feedstock, as it was
236 concluded in other previous studies employing different types of wastes¹⁰. On average,
237 VS and COD_T removal in all the cases was 44.6 and 49.9% for SS and 52.7 and 56.7%
238 for SS:WDW for OLR ≤ 3.2 (kg_{VS}/m³·d).

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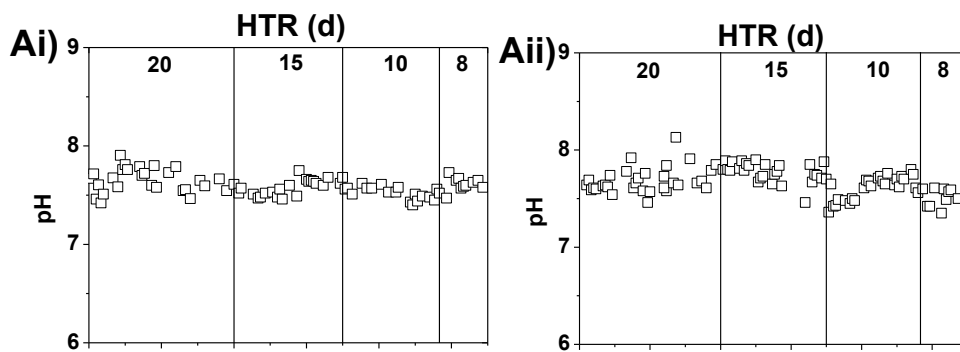
240 Total VFA (mgAc/L) at the steady state is also shown in Table 2. There is a slight
241 increase between 20 and 8 d HRT of the total VFA concentration, being higher in co-
242 digestion digesters than in those fed only with SS. Taking into account that initial VFA

243 were very high (4424 ± 122 mg Ac/L and 6827 ± 135 mg/L Ac/L for WDW:SS and SS,
 244 respectively) the VFAs were used almost fully: between 76-90% and 90-96% for
 245 WDW:SS and SS, respectively. It should be pointed out that this parameter had no
 246 effect on pH, which remained stable during the tests. According to these results, the co-
 247 digestion system has proven to be stable under the operating conditions studied here.

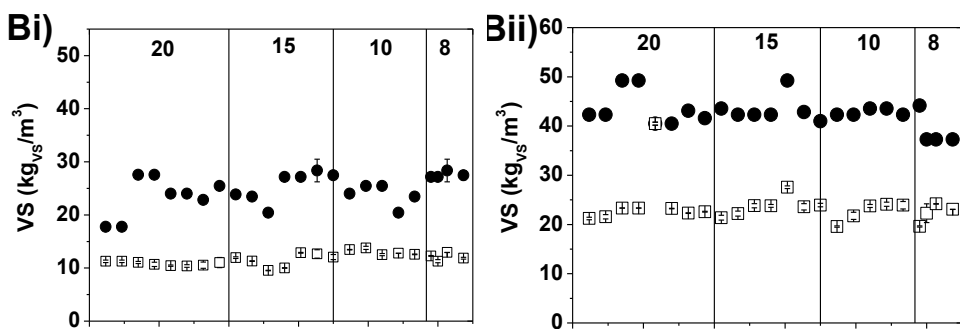
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249 In Table3, VS/TS ratios are also shown, obtaining on average $61.4\% \pm 2.0$ and $71.2 \pm$
 250 1.3% for SS:WDW and SS, respectively. Regarding energy efficiency (EE) as the
 251 energy cost of recovering usable energy from the sludge, according to Li and Feng
 252 (2018)³⁰ when AD is operating at $VS/TS \geq 60\%$, the system was more than twice
 253 efficient than the

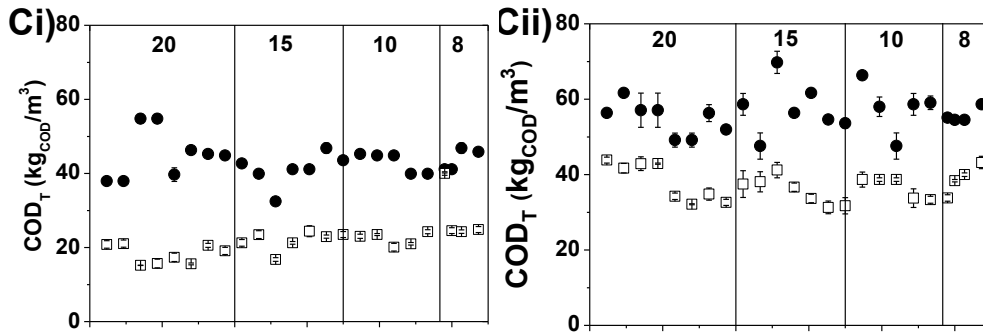
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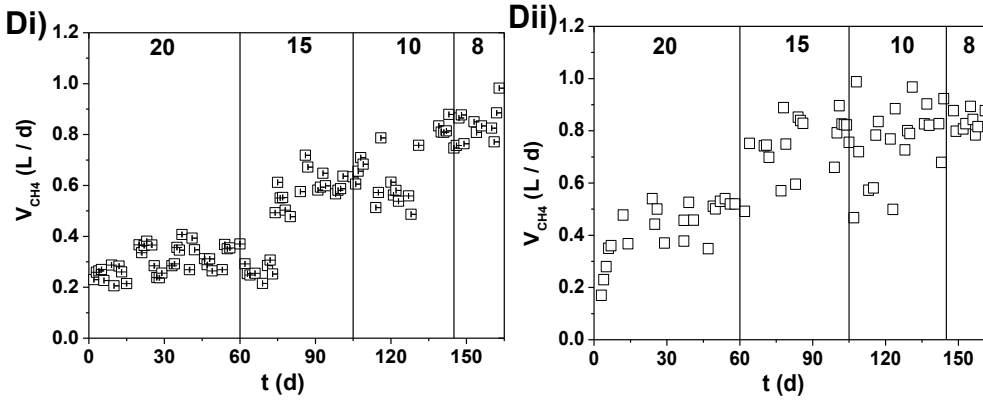
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256



257



258 **Figure 1.** Evolution of (A) pH inside the digesters, (B) VS of the feedstock and the
 259 effluent, (C) COD of the feedstock and the effluent, and (D) daily methane volume in
 260 the semi-continuous anaerobic digesters of (i) SS:WDW (1:1 (v/v)), and (ii) SS. Key
 261 ●feeding □effluent.

system working at VS/TS = 70%. Then, the ACoD system proposed not only will be an eco-friendly way of wine making residue valorization but also an energetically efficient process.

Table 3. Main characteristic of the effluents and daily methane production at the steady state: (a) 1:1, SS:WDW and (b) SS.

HTR (d)	VS (kgvs/ m ³)	VS/TS (%)	CODt (kgcod/ m ³)	CODs (kgcod/ m ³)	VFAs (mg _{ac} /L)	V _{CH4} (L/d)	X _{CH4} (%)
20	10.6 ± 0.1	59.9	15.2 ± 0.9	8.5 ± 0.5	418 ± 87	0.47 ± 0.03	68.1 ± 1.6
15	11.3 ± 0.7	60.4	16.8 ± 1.4	8.8 ± 0.9	721 ± 60	0.63 ± 0.03	66.8 ± 1.1

10	12.7 ± 0.1	64.8	20.6 ± 0.1	9.6 ± 0.8	1018 ± 103	0.75 ± 0.06	68.0 ± 1.4
8	12.2 ± 0.5	60.4	22.4 ± 5.2	10.5 ± 2.3	1608 ± 189	0.92 ± 0.01	69.4 ± 1.6

262 (a)

HTR (d)	VS (kg _{vs} / m ³)	VS/TS (%)	COD _t (kg _{cod} / m ³)	COD _s (kg _{cod} / m ³)	VFA _s (mg _{ac} /L)	V _{CH₄} (L/d)	X _{CH₄} (%)
20	22.7 ± 0.4	70.5	28.9 ± 1.9	17.3 ± 0.9	271 ± 69	0.54 ± 0.03	68.8 ± 2.4
15	23.1 ± 0.4	70.2	31.5 ± 1.8	14.7 ± 0.5	398 ± 90	0.82 ± 0.02	68.3 ± 1.5
10	23.2 ± 0.7	70.5	36.1 ± 1.5	15.0 ± 2.6	446 ± 76	0.89 ± 0.01	68.0 ± 2.9
8	23.3 ± 0.4	73.5	38.2 ± 1.6	14.0 ± 0.5	658 ± 102	0.93 ± 0.01	67.7 ± 1.2

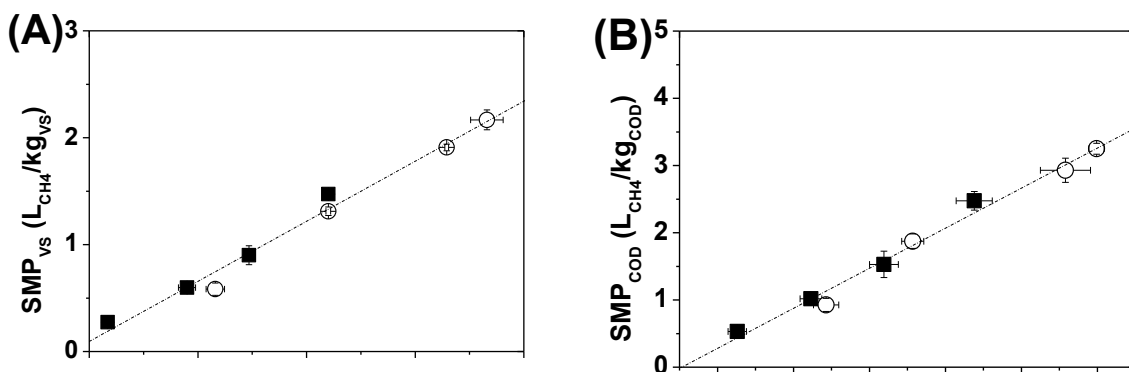
263 (b)

264 3.3 Biogas production

265 Figure 1-D (i, ii) shows the evolution of daily methane production. In response to
 266 changing OLR conditions, an acclimation stage is observed before to reaching the
 267 steady state. The lower the HRT (which means the higher the OLR), the higher the
 268 biogas production. The average methane production under each condition is
 269 summarized in Table 2. The maximum value obtained was 0.92 ± 0.2 L/d at 8 d HRT,
 270 regardless of substrate used. Table 2 also shows the percentage of methane contained in
 271 the biogas (X_{CH₄}), near of 70% in both trials, similar than previous reported by ACoD of
 272 these both substrates¹⁷.

273 The influence of OLR on specific methane production (SMP) in terms of VS and COD
 274 are shown in Figure 2 (A, B). Increasing OLR lead to a linear increase in SMP,
 275 regardless of the waste employed (SS:WDW or SS). However, as it can be seen in
 276 Figure 2 (C, D) the influence of OLR on MP shows a different trend. ACoD of
 277 SS:WDW significantly enhances MP with respect to AD of SS alone in terms of both
 278 VS and COD, because initial SS had more VS and COD than SS:WDW (Table 1) . The

279 explanation of this result lies in the favourable characteristics of WDW (high dissolved
 280 organic matter content and biodegradability) improving methane production rate. The
 281 reduced effectiveness of the system is also reflected in the higher accumulation on VFA
 282 intermediate compounds in the AD (Table 2). Based on these results, employing HRT
 283 below 8 d could entail the destabilization of the digester and the breakdown of
 284 efficiency. The best methane productivity was obtained when ACoD of SS:WDW was
 285 operated at HRT = 8d (OLR = 3.2 kg_{VS}/m³·d), obtaining 18.0 L<sub>CH₄}/kg_{VS}·d and 10.7
 286 L<sub>CH₄}/kg_{COD}·d, being 30% higher than those observed in the AD of SS alone. Other
 287 researchers have obtained similar MP increases on mono-digestion of SS by addition of
 288 agri-food residues. Donoso-Bravo et al.,³¹ studied the effect of ACoD of SS with two
 289 co-substrates: (i) beverage wastewater and (ii) thermally pretreated biological sludge.
 290 Results obtained improved values of MP in 21.4% and 16.2% by using 10% v/v of co-
 291 substrates and 90% of SS. Montañés et al.,³² obtained 33.6% higher MP in terms of
 292 m³CH₄/kg COD_{removal} by using 10% v/v of leaching of sugar beep pulp as co-substrate at
 293 OLR = 3.55 kg_{VS}/m³·d. Pitk et al.,³³ obtained an increase of 37.7% at OLR ~ 3
 294 kg_{VS}/m³·d using 7.5% of slaughterhouse residues.
 295</sub></sub>



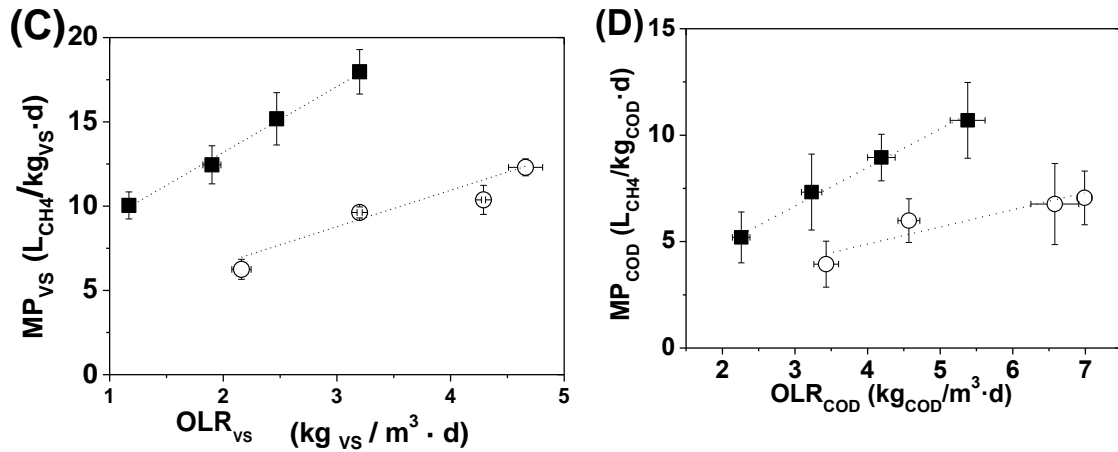


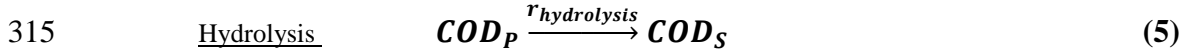
Figure 2 Influence of OLR on (A) SMP in terms of VS, (B) SMP in terms of COD, (C) MP in terms of VS and (D) MP in terms of COD. *Key:* ■SS:WDW (1:1) ○SS.

296 3.4 Kinetic modelling

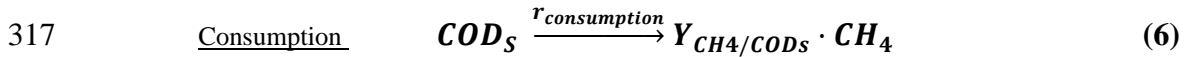
297 A kinetic model is proposed based on the MP results to describe the step rates involved
 298 in both the ACoD of SS:WDW and the AD of SS alone. AD takes places via a complex
 299 biological reaction network. An unstructured non-segregated kinetic model is proposed
 300 here to describe the anaerobic digestion of WDW and SS at the macroscopic scale. The
 301 two reactions considered are: hydrolysis of the solid substrate (COD_p) to obtain
 302 accessible substrate (COD_s) for the microorganisms (Eq. 5), and consumption of this
 303 accessible substrate to produce methane (Eq. 6). The Eq. 5 simplify the equations
 304 produced during the hydrolysis because the exo-enzymes activity of microbes. In this
 305 sense, the organic matter particulate (measured as COD_p) is converted to organic matter
 306 soluble (COD_s). On the other hand, the Eq. 6 simplify in a unique reaction the organic
 307 matter consumption reactions that produce biomethane. This reaction schematically
 308 represents all the processes that occur when biodegradable organic matter (which
 309 indirectly is measured by COD_s) is converted to biomethane (CH₄). It is necessary to
 310 establish a relationship between both parameters with the stoichiometric coefficient.
 311 This parameter is analogue to biomethane yield. As it is known, that this complex

312 process does not occur in a unique step, this yield involves the stoichiometry in
 313 macroscopic terms.

314



316



318

319 The proposed kinetic equations depend on the substrate concentration via a first-order
 320 reaction (Eq. 7 and 8), in line with previously published papers by other authors³⁴⁻³⁶.

321

322 Hydrolysis $r_{hydrolysis} \left(\frac{kg_{COD}}{m^3 \cdot d} \right) = k_{hydrolysis} \cdot COD_P$ (7)

323

324 Consumption $r_{consumption} \left(\frac{kg_{COD}}{m^3 \cdot d} \right) = k_{consumption} \cdot COD_S$ (8)

325

326 Considering the mass balance in the digester and assuming that the digester behaves as
 327 an ideal complete mixed tank bioreactor, the hydrolysis and consumption rates are
 328 related to properties of the feedstock and effluent at the steady state, and the HRT
 329 condition. Therefore, both rates can be calculated using inlet and outlet biodegradability
 330 parameters (Table 2) at the steady state for each HRT condition (Eq. 9 and 10).
 331 According to Eq. 9 $r_{hydrolysis}$ is calculated by difference of inlet and outlet COD_p (which
 332 represent the soluble matter formed inside the reactor) referred to HRT. However, in
 333 Eq.10 the consumption rate shows the difference between CODs in the reactor (CODs
 334 that enter with feeding plus the CODs that already is inside the reactor as a consequence
 335 of hydrolysis step) and the CODs that exit from reactor.

336

337 Hydrolysis $r_{hydrolysis} = \frac{1}{HRT} \cdot (COD_P^{Inlet} - COD_P^{Outlet})$ (9)

338

339 Consumption $r_{consumption} = \frac{1}{HRT} \cdot (COD_S^{inside reactor} + COD_S^{inlet}) - COD_S^{Outlet}$

340 (10)

341

342 Based on these equations, the kinetic parameters of the model ($k_{hydrolysis}$ and $k_{consumption}$)
 343 and the pseudo-stoichiometric parameter ($Y_{CH_4/COD}$) can be estimated (Table 3) by
 344 fitting the experimental data (Figure 3) to linear regression.

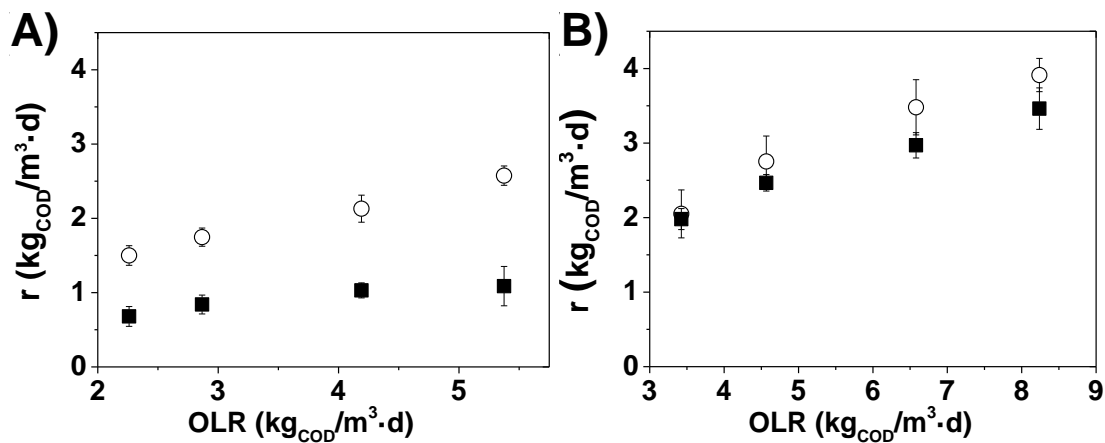
345

346 In Figure 3 it is shown the evolution of reaction rate in each step (Hydrolysis and
 347 consumption) at each condition: mono-digestion of SS and co-digestion of SS:WDW. In
 348 the case of SS condition (Figure 3-B) the hydrolysis and consumption rate are very
 349 similar. This occurs because the hydrolysis was the rate-limiting step since the SS
 350 contains a high number of complex structures that must be hydrolyzed before the rest of
 351 the process and hence the consumption step depends on hydrolysis. Taking into account
 352 the consumption rate calculation (Eq. 9), two effects occurred in mono-digestion of SS:
 353 (1) CODs inlet was low because low content of easily hydrolyzable compounds in SS so
 354 $K_{hydrolysis}$ must be high for transforming the major number of complex structures to
 355 simple ones (2) acetogenesis is quicker than hydrolytic-acidogenesis³⁷ so: in spite of
 356 high activity of hydrolysis transforming CODp into CODs, the consumption of CODs is
 357 higher than the production. So, in the calculation of $K_{consumption}$ it is important to take
 358 into account that the majority of CODs formed (CODs inside the reactor, Eq.10) is
 359 assimilated. And hence, its concentration measured in the reactor is very low (only
 360 0.04-1% of substrate CODs, Table 2) and the sum with the inlet CODs is lower than
 361 CODs outlet obtaining a negative $K_{consumption}$ (Table 4).

362

363 However, in the case of co-digestion of SS:WDW (Figure 3-A) , the hydrolysis rate
364 was higher than consumption one, due to the high amount of easily biodegradable
365 compounds supply by WDW co-substrate. So in this case, the hydrolysis was not the
366 limiting-step (as it usually happens in AD) because the WDW contribute directly with
367 easily hydrolyzable organic matter compounds (inlet CODs, in Eq. 10). In addition, the
368 higher amount of TVS in WDW enhance the nutrients matter transfer to
369 microorganisms³⁷. Other authors have previously identified the degradation of acetate
370 (an intermediate compound in the metabolic pathway) as the rate-limiting step in co-
371 digestion processes ³⁸⁻³⁹. As acetate assimilation is one of the reactions that occur during
372 consumption process, in this case, the rate-limiting step can be the consumption step
373 and $K_{hydrolysis}$ was higher than $K_{consumption}$ (Table 4).

374



375

376

377 **Figure 3** Influence of OLR on the hydrolysis and consumption reactions rate in the
378 AcoD digester of SS:WDW (1:1 (v/v)) and in the control digester: (A) SS:WDW (1:1
379 (v/v)). and (B) SS. Key: ○hydrolysis ■consumption.

380

Table 4 Values of the kinetic and stoichiometric parameters obtained by regression using the first kinetic model, Eq. (5-8).

Feedstock	Parameter	Value	r ²	SSR
Co-digestion (1:1; SS:WDW)	$k_{hydrolysis} (d^{-1})$	$5.22 \cdot 10^{-1}$	0.996	0.0102
	$k_{consumption} (d^{-1})$	$9.57 \cdot 10^{-2}$	0.962	0.0044
	$Y_{CH_4/COD} (kg_{CH_4}/kg_{COD})$	$1.15 \cdot 10^{-1}$	0.966	0.0004
Digestion (SS)	$k_{hydrolysis} (d^{-1})$	$1.65 \cdot 10^{-1}$	0.997	0.0250
	$k_{consumption} (d^{-1})$	$-4.98 \cdot 10^{-1}$	0.833	0.0346
	$Y_{CH_4/COD} (kg_{CH_4}/kg_{COD})$	$0.95 \cdot 10^{-1}$	0.999	0.0020

381

382 Comparing both conditions, in spite of having a $k_{hydrolysis}$ in the same order in both
 383 conditions, the high $k_{consumption}$ in the case of co-digestion increase the global rate of the
 384 process obtaining a higher stoichiometric parameter for SS:WDW (0.165 kg_{CH_4}/kg_{COD})
 385 than that for SS (0.094 kg_{CH_4}/kg_{COD}). Then, ACoD of SS:WDW improved the
 386 biomethane potential and hence also the methane production efficiency of the systems
 387 removing the limiting effect of hydrolysis step.

388 Finally, the available organic matter consumption (elimination of COD_p) and
 389 production (production of COD_s) were calculated by Eq. 11 and 12, respectively; and
 390 the methane production by Eq. 13; taking into account its roles in the net of reactions
 391 proposed in the kinetic model as well as the kinetic values of constant (k) at the steady
 392 state in the semi-continuous anaerobic digesters. The results were drawn-up in Figure 4,
 393 evaluating the influence of HRT on each of them.

394

395 Solid substrate consumption $(-R_{CODp}) = r_{hydrolysis}$ **(11)**

396

397 Soluble substrate consumption $(-R_{CODs}) = r_{hydrolysis} - r_{consumption}$ (12)

398

399 Methane production $R_{CH4} = Y_{CH4/CODs} \cdot r_{consumption}$ (13)

400

401 As it was explained before, the ACoD of SS:WDW (1:1 v/v) avoid the limiting effect of
402 hydrolysis step and as it was expected, the solid substrate consumption rate was much
403 higher than the soluble substrate consumption being the consumption the rate-limiting
404 step. In short, adding WDW to the feedstock involves a switch in the rate-limiting step
405 in the process due to the high dissolved organic matter contained in this waste. Then, for
406 ACoD of SS:WDW (1:1 v/v) the methane production rate depend on the consumption
407 rate mainly because acetate degradation limiting effect.

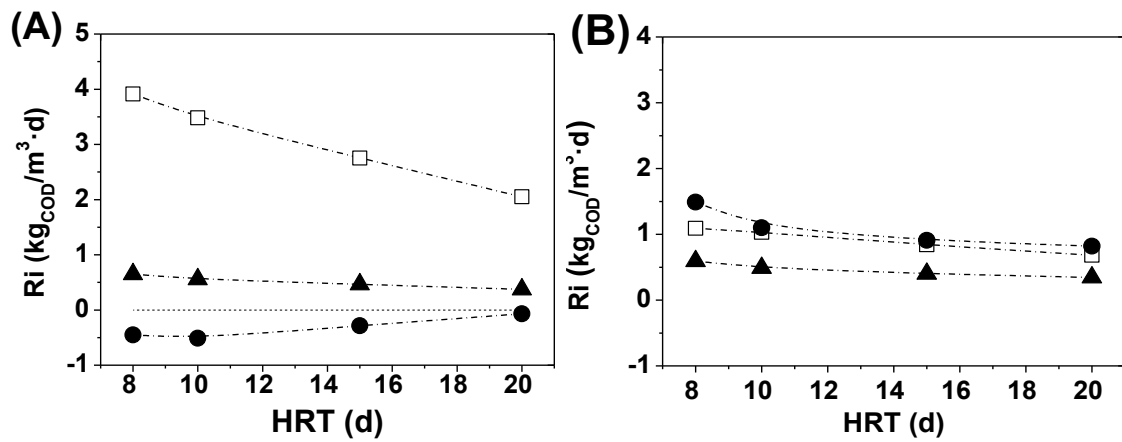
408

409 When sole SS was used as substrate, the CODp and CODs were very similar and it was
410 reduced with the increasing of HRT (Figure 4-A). However, in this case of the methane
411 production obtained lower values than hydrolysis or solid/soluble substrate
412 consumption. This means that not only hydrolysis but also methanogenesis is the rate-
413 limiting step in this process. This occur because the high sensibility of the *Archaea*
414 microorganisms to changes in the environment as well as the diffusional limitations of
415 biomethane in the liquid medium ⁴⁰⁻⁴². Therefore, the control of the biomethane
416 production in SS mono-digestion was due to the hydrolysis and methanogenesis steps.

417

418 In spite of being hydrolysis step the rate-limiting step in SS mono-digestion, in both
419 conditions, the highest rates of methane production were reached at minimum OLR
420 (Figure 3) and at maximum HRT = 8d (Figure 4) because the augmentation of new
421 organic compounds used for microbial population.

422



423

424 **Figure 4** Influence of HRT on consumption rates in the semi-continuous anaerobic
425 digesters of (A) SS:WDW (1:1 (v/v)), and (B) SS. Key: \square COD_P \bullet COD_S \blacktriangle CH_4 .

426

427 4 Conclusions

428 The proposed ACoD system promotes efficiently wine-making industry water
429 sustainability by its use in WWTP as a co-substrate with sewage sludge. When
430 SS:WDW was anaerobically digested, biodegradability of the mixture in terms of VS
431 and CODT was 7-8% higher (52.7 and 56.7%, respectively for $OLR \leq 3.2$ ($kg_{VS}/m^3 \cdot d$))
432 and methane production was 30% higher than when SS was used as sole substrate. It
433 was reflected in kinetic study results that co-digestion improved biomethane potential
434 and methane production efficiency by switching the rate-limiting step. In this sense,
435 methane production related to the amount of organic matter was higher in the AcoD
436 SS:WDW (0.165 kg_{CH_4} / kg_{COD}) than in AD of SS alone (0.096 kg_{CH_4} / kg_{COD}).
437 These results open a new path in optimization studies of WWTP design and operation
438 by using new agro-industrial residues in an eco-friendly way.

439

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443 *from biosolids and vinasses anaerobic co-digestion*, financed by the European Regional
444 Development Fund (ERDF).

445 **Nomenclature**

446	AD	Anaerobic digestion
447	COD	Chemical oxygen demand (kg/m ³)
448	COD _P	Particulate chemical oxygen demand (kg/m ³)
449	COD _S	Soluble chemical oxygen demand (kg/m ³)
450	COD _T	Total chemical oxygen demand (kg/m ³)
451	EE	Energy efficiency
452	HRT	Hydraulic retention time (d)
453	<i>k</i>	Kinetic constant (d ⁻¹)
454	MP	Methane productivity (L/kg·d)
455	OLR	Organic loading rate (kg/m ³ ·d)
456	<i>r</i>	Reaction rate (kg/m ³ ·d)
457	R	Production rate (kg/m ³ ·d)
458	SMP	Specific methane production (L/kg)
459	SS	Sewage sludge
460	TS	Total solids (kg/m ³)
461	V	Volume (L)
462	VFA	Volatile fatty acids (mg/L)
463	VS	Volatile solids (kg/m ³)
464	WDW	Wine distillery wastewater
465	WWTP	Wastewater treatment plant
466	X _{CH₄}	Percentage of methane in the biogas (%)
467	Y	Stoichiometric parameter
468	Subscript	
469	COD	Relating to chemical oxygen demand

470	<i>Consumption</i>	Relating to the consumption reaction
471	CH ₄	Relating to methane
472	Digester	Relating to the operating volume
473	<i>Hydrolysis</i>	Relating to the hydrolysis reaction
474	i	Relating to compound i
475	<i>Inlet</i>	Relating to the feed stream
476	<i>Outlet</i>	Relating to the effluent stream
477	VS	Relating to volatile solids
478		

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603

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611

612

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618 **Figure 2** Influence of OLR on (A) SMP in terms of VS, (B) SMP in terms of
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620 **Figure 3** Influence of OLR on the hydrolysis and consumption reactions rate in the
621 AcoD digester of SS:WDW (1:1 (v/v)) and in the control digester: **(A)**
622 SS:WDW (1:1 (v/v)), and **(B)** SS. Key: ■ *consumption*. ○ *hydrolysis*

623 **Figure 4** Influence of HRT on production rates in the semi-continuous anaerobic
624 digesters of **(A)** SS:WDW (1:1 v/v) and **(B)** SS.

625 **Figure Captions**

626 **Figure 1** Key ● *feed* ■ *effluent*.

627 **Figure 2** Key: ■ SS:WDW (1:1) ○ SS.

628 **Figure 3** Key: ○ *hydrolysis* ■ *consumption*

629 **Figure 4** Key: □ COD_P ● COD_S ▲ CH_4 .