

1 **Comparison of cranial sex determination by discriminant**  
2 **analysis and logistic regression**

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9 8 tables

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11 **Abstract**

12 Various methods have been proposed for estimating dimorphism. The objective of  
13 this study was to compare sex determination results from cranial measurements using  
14 discriminant analysis or logistic regression. The study sample comprised 130  
15 individuals (70 males) of known sex, age, and cause of death from San José cemetery in  
16 Granada (Spain). Measurements of 19 neurocranial dimensions and 11 splanchnocranial  
17 dimensions were subjected to discriminant analysis and logistic regression, and the  
18 percentages of correct classification were compared between the sex functions obtained  
19 with each method. The discriminant capacity of the selected variables was evaluated  
20 with a cross–validation procedure. The percentage accuracy with discriminant analysis  
21 was 78.2% for the neurocranium (82.4% in females and 74.6% in males) and 73.7% for  
22 the splanchnocranium (79.6% in females and 68.8% in males). These percentages were

23 higher with logistic regression analysis: 85.7% for the neurocranium (in both sexes) and  
24 94.1% for the splanchnocranium (100% in females and 91.7% in males).

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26 **Keywords:** neurocranium; splanchnocranium; sex determination; discriminant function  
27 analysis; logistic regression; sexual dimorphism

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## 42 **Introduction**

43 Sex determination is the cornerstone for establishing a biological profile of human  
44 remains (Rogers, 2005). Traditional studies based on morphological characteristics  
45 encounter some difficulties, because many features depend on the observer, the  
46 nutritional status, occupation, and/or origin (Devang et al., 2015). Anthropometric  
47 methods are more reliable for sexing when adequate reference data (formulae) are  
48 available for the study population.

49 A complete description of logistic regression is provided by Albanese (2003), who  
50 suggests useful approaches for evaluating the fit of a logistic model to the data. Logistic  
51 regression differs from discriminant function analysis because it does not require a  
52 normal distribution of independent variables and is less sensitive to strong correlations  
53 among predictor variables (Press and Wilson, 1978; Albanese, 2003; Pohar et al., 2004;  
54 Acharya et al., 2011). Logistic regression is more flexible in its assumptions and  
55 delivers a better performance, even when the assumptions of discriminant function  
56 analysis are met (Albanese, 2003; Acharya et al., 2011).

57 Nevertheless, logistic regression is only rarely used in physical anthropology or  
58 forensic medicine for sex assessment from measurements, and discriminant function  
59 analysis has been applied by most authors. Thus, numerous authors employed the latter  
60 method to estimate the sex of individuals using craniometric variables, including  
61 bizygomatic width, basion-bregam height, nasal height and width, facial length and  
62 width, and/or maxillary-alveolar length and width (Cunha and Van Vark, 1991; Song,  
63 1992; Steyn, and Iscan, 1998; Rosique et al., 2004; Franklin et al., 2005; Deshmukh and  
64 Devershi, 2006; Kemkes and Göbel, 2006; González et al., 2009). The percentage of  
65 correct sex allocation obtained by these authors ranged between **72.15 and 96.7%**.

66 Logistic regression can be used as an alternative option when predictor variables do  
67 not have equal variance-covariance matrices. Logistic regression functions developed  
68 for sex determination correctly classified 74.5% of individuals studied by Casas et al.  
69 (2009), who considered 5 dental variables and 88% of those studied by Walker (2008),  
70 who studied a series of cranial variables In a study to determine sex from the teeth of  
71 adults, Acharya et al. (2011) reported 91% sex allocation accuracy using logistic  
72 regression and only 62.9% accuracy using discriminant analysis, concluding that the  
73 former was superior for dental sex assessment.

74 The purpose of the present study was to compare the accuracy of sex identification  
75 from cranial measurements between two statistical approaches: discriminant analysis  
76 and logistic regression.

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## 78 **Material and methods**

79 This study included adult skeletons of known sex, age, and cause of death from the  
80 San José collection, kept in the Physical Anthropology Laboratory of the University of  
81 Granada and derived from the municipal cemetery of Granada city (Southern Spain).

82 The study sample comprised skulls from 130 Mediterranean individuals (70 males  
83 and 60 females) who died in Granada during the 20<sup>th</sup> century. The mean age was 69  
84 years (range, 22-93 years). Because of the advanced age of many of these individuals  
85 and the resulting alterations in the mandibular region (from tooth losses and consequent  
86 alveolar resorption) and frequent presence of disease, measurements of this region were  
87 not considered in the present study. For the same reason, it was not possible to measure  
88 BPL, UFH, and MAL variables (see Table 1 for abbreviations) in all of the individuals  
89 studied. Measurements were taken with a digital caliper (accuracy of 0.01 mm) by the

90 same examiner (A.A-A.) and repeated after a 15–day interval to test the intra-observer  
91 error, considered a sufficient time interval to ensure that the second assessment was not  
92 influenced by learning acquired at the first examination (Viciano et al., 2013). A second  
93 observer used the same caliper to measure the same dimensions in 30 randomly selected  
94 individuals in order to assess the inter-observer error. Table 1 displays the cranial  
95 measurements taken, following Martin and Kunsmann (1988).

96

97 (Insert Table 1)

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99 SPSS 15.0 (IBM, Chicago, IL) was used for the data analyses. Data were expressed  
100 as means with standard deviations, and the normality of their distribution was assessed  
101 using the one-sample Kolmogorov–Smirnov test. The intraclass correlation coefficient  
102 (ICC) was used to evaluate the intra- and inter-observer agreement, estimating the mean  
103 of correlations between all possible pairs of observations. The ICC classification (range  
104 0–1) proposed by Fleiss (1986) was adopted. Repeated–measures analysis of variance  
105 (ANOVA) was performed to assess the statistical significance of the variability between  
106 pairs of measurements.

107 A *t*–test was used to compare data between the sexes and evaluate the homogeneity  
108 of variance (*F*–test). Dimensions showing no significant differences between sexes were  
109 excluded from subsequent statistical models. The effectiveness of the cranial  
110 dimensions for sex determination was first determined by discriminant function  
111 analysis, using a stepwise procedure to select the variables with the highest discriminant  
112 capacity. An M-Box test was performed to determine whether the covariance matrices  
113 were homogeneous. A cross–validation procedure re-calculated the discriminant  
114 function analysis, sequentially and randomly selecting one of the samples and averaging

115 the results across all cross-validation values. Next, logistic regression analysis was  
116 separately performed to identify the most useful sex discrimination functions. Equations  
117 were calculated for pairs of measurements (considering all dimensions) in order to  
118 maximize the applicability of the technique for archaeological and forensic cases in  
119 which the cranium is incomplete or poorly preserved. The  $-2 \log$  likelihood was  
120 calculated to assess the fit of logistic regression models to the data (lower  $-2 \log$   
121 statistic = better fit). Discriminant analysis function and logistic regression were  
122 separately performed for the neurocranial and splanchnocranial variables.

123

## 124 **Results**

125 The data for males and females were separately checked with the Kolmogorov–  
126 Smirnov test, which showed that all dimensions were normally distributed ( $t$ -test,  $P >$   
127  $0.05$ ). The ICC results ( $ICC \geq 0.75$ ;  $p > 0.05$ ) demonstrated that the measurements were  
128 generally highly reproducible, with an elevated precision and accuracy (Fleiss, 1986).

129 Table 3 reports the mean values recorded for all dimensions. Student's  $t$ -test results  
130 revealed statistically significant differences ( $P < 0.05$ ) between the sexes in 6 of the 11  
131 splanchnocranial dimensions and in 12 of the 19 neurocranial dimensions (Table 2).

132

133 (Insert Table 2)

134 Table 3 lists the coefficients, the classification functions for neurocranium and  
135 splanchnocranium, the  $F$  and Wilks' lambda values, and the discriminant functions with  
136 corresponding sectioning points. The M-Box test showed homogeneous covariance  
137 matrices ( $P > 0.05$ ). The discriminant analysis yielded six functions for the  
138 neurocranium and only one for the splanchnocranium. Discriminant analysis selected

139 BBH, MCL, LIA, TSA, and ABH (see Table 3) for the neurocranium and BizB for the  
140 splanchnocranium as having the greatest discriminant power. Females and males could  
141 be readily differentiated, and the centroids markedly differed between the sexes.

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143 (Insert Table 3)

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145 The reliability (classification accuracy) values obtained for these functions are given  
146 in Table 4. The cross-validation procedure showed a mean reliability of 78.2% (82.4%  
147 in females and 74.6% in males) for the neurocranium and 73.7% (79.6% in females and  
148 68.8% in males) for the splanchnocranium (Table 4). Univariate discriminant analysis  
149 of BBH (function 2), MCL (function 3), LIA (function 4), TSA (function 5), and ABH  
150 (function 6) revealed that the sexual dimorphism was highest for the BBH and lowest  
151 for the LIA (Table 4). The highest percentage sex classification accuracy was obtained  
152 with the BBH dimension.

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155 (Insert Table 4)

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157 Table 5 exhibits the logistic regression coefficients for each function. Five functions  
158 were obtained for the neurocranium and one for the splanchnocranium. Logistic  
159 regression selected MCL, BBH, TSA, and LIA for the neurocranium and BizB for the  
160 splanchnocranium. With this model, the percentage classification accuracy was 85.7%  
161 (in both sexes) for the neurocranium and 94.1% (100% in females and 91.7% in males)  
162 for the splanchnocranium (Table 5). In the case of the neurocranium, the same  
163 percentage of correct classification (85.7%) was obtained for the males than for the

164 females; however, in the case of the splanchnocranium, this percentage was higher for  
165 the females (100%) than for the males (91.7%) (Table 6).

166 .

167 (Insert Table 5)

168 (Insert Table 6)

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170 Univariate logistic regression results for MCL (Function 2), BBH (function 3), TSA  
171 (function 4), and LIA (function 5) showed the highest sexual dimorphism for BBH and  
172 the lowest for LIA (Table 5). Table 6 displays the data on the classification accuracy of  
173 these functions. In the paired logistic regression analyses, BBH was selected for all  
174 neurocranial functions, while BizB was the most frequent (79.5-94.1%) among  
175 splanchnocranial functions (Table 7). Both methods selected MCL, BBH, TSA, and  
176 LIA for the neurocranium and BizB for the splanchnocranium, although the percentages  
177 of correct classification differed between the statistical approaches.

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179 (Insert Table 7)

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## 181 **Discussion**

182 In this study of 130 adult skeletons, significant differences were found between the  
183 crania of females and males, in agreement with previous reports (Paiva and Segre, 2003;  
184 Kemkes and Göbel, 2006).

185 Most of the dimensions were selected by both discriminant analysis and logistic  
186 regression and can be considered useful for sex determination. The majority of these  
187 were previously identified as key variables by different authors, including: MCL by

188 Song (1992), Steyn and Iscan (1998), Fernández (2007), and Zabando et al. (2009);  
189 BBH by Krenzer (2005) and Franklin et al. (2005); and BizB by Giles and Elliot (1963),  
190 Song (1992), Steyn and Iscan (1998), Rosique et al. (2005), and Zabando et al. (2009).

191 In the discriminant analysis, the percentage sex classification accuracy was higher  
192 for neurocranial than splanchnocranial measurements. This may reflect a higher  
193 effectiveness when five dimensions are considered (BBH, MCL, LIA, TSA, ABH)  
194 rather than only one (BizB). In contrast, the percentage classification accuracy was  
195 higher for the splanchnocranium in the logistic regression analysis and would be the  
196 optimal region for sex determination using this approach.

197 The percentages of correct sex classification obtained with discriminant analysis  
198 slightly differed from those published by other authors using this statistical method.  
199 Thus, percentages of 85.6-89.7% were reported by Hanihara (1958) in a study of 9  
200 cranial variables in a Japanese population and percentages of 80-86% by Steyn & Iscan  
201 (1998) in an examination of 91 South African skulls. Sanjai et al. (2007) used logistic  
202 regression in a study of 101 Thaiandese skulls and obtained a percentage accuracy of  
203 88.8%. The small variations among studies may be attributable to differences in sample  
204 size or in the origin of the samples.

205 The percentages of correct classification were higher for females than for males with  
206 both methods and in both cranial regions. All of the selected variables would have  
207 greater discriminant power in females than males. In general, it has been reported that  
208 males are more affected by diseases, malnutrition, and climatic events (Suazo et al.,  
209 2008), and Pucciarelli et al. (1990) demonstrated that growth patterns were more  
210 strongly influenced by environmental conditions in males than in females. However,  
211 these gender differences may vary among populations.

212 BBH and BizB proved to be the most useful sex determination variables in both  
213 analyses. In the paired logistic regression and univariate discriminant analysis, they  
214 achieved the highest classification percentages and were the most frequently repeated  
215 variables, and they showed the greatest weight when the multivariate function was  
216 applied. These were found to be the best cranial variables for sex determination by  
217 various authors, including Giles and Elliot (1963), Song (1992), Steyn and Iscan (1998),  
218 Krenzer (2005), Franklin et al. (2005), Rosique et al. (2005), and Zabando et al. (2009).

219 The percentage correct classification was higher with logistic regression than with  
220 discriminant analysis. Logistic regression appears to be a useful method for sex  
221 determination from cranial measurements in the absence of other bones with identifiable  
222 sex-specific characteristics (Albanese, 2003; Sangvichien, 2007).

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## 224 **Conclusions**

225 The findings of this study indicate that logistic regression is the most useful method  
226 to determine sex from cranial measurements. In this Mediterranean population, the BBH  
227 and BizB offered the greatest discriminant power for sex determination. According to  
228 the logistic regression results, the optimal cranial region for sex determination is the  
229 splanchnocranium. This approach is of particular interest to anthropologists, because it  
230 can be used to determine the sex of skeletons when only part of the cranium is  
231 preserved.

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